

Scalable synchronization of spin-Hall oscillators in out-of-plane field

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A strategy for a scalable synchronization of an array of spin-Hall oscillators (SHOs) is illustrated. In detail, we present the micromagnetic simulations of two and five SHOs realized by means of couples of triangular golden contacts on the top of a Pt/CoFeB/Ta trilayer. The results highlight that the synchronization occurs for the whole current region that gives rise to the excitation of self-oscillations. This is linked to the role of the magnetodipolar coupling, which is the phenomenon driving the synchronization when the distance between oscillators is not too large. Synchronization also turns out to be robust against geometrical differences of the contacts, simulated by considering variable distances between the tips ranging from 100 nm to 200 nm. Besides, it entails an enlargement of the radiation pattern that can be useful for the generation of spin-waves in magnonics applications. Simulations performed to study the effect of the interfacial Dzyaloshinskii-Moriya interaction show nonreciprocity in spatial propagation of the synchronization make this design of array of SHOs scalable for a larger number of synchronized oscillators. *Published by AIP Publishing*. [http://dx.doi.org/10.1063/1.4967842]

Microwave oscillators are widely employed in modern technology.¹ For example, in wireless high-speed communications, they provide the clocking of the systems, as well as the generation of the carrier waves. The most common type of semiconductor microwave oscillators is the voltage-controlled oscillator (VCO).² It exhibits high operating frequencies (over 100 GHz), low cost, and low power consumption; nonetheless, it holds limited tunability (±20%).^{3,4} Microwave spin-transfer-torque nano-oscillators (STNOs)⁵⁻⁸ and spin-Hall oscillators $(SHOs)^{9-12}$ seem to be promising as solutions beyond VCOs that are also compatible with the complementarymetal-oxide silicon (CMOS) technology. In addition to low cost, low power consumption and high output frequencies, they offer a tunability, wider than VCO, on current and magnetic field.^{8,13} Other features are: better scalability (over 50 times smaller), high quality factors,¹⁴ stability in a broad range of temperatures, intrinsic radiation hardness. On the other hand, the main weakness of STNOs and SHOs is the low output power (order of microwatts for the magnetic tunnel junction STNO).^{13,15} This limitation can be overcome by the synchronization of a number of oscillators. With this regard, Kaka et al.¹⁶ and Mancoff et al.¹⁷ authored two milestone papers where the first experimental observation of two phaselocked nano-contact STNOs was demonstrated. The synchronization was considered mutual since each oscillator participated actively in the phenomenon, and, among the results, it entailed the desired increase of the output power and a reduction of linewidth. Starting from those papers, the synchronization of STNOs has been studied diffusely, theoretically,^{18,19} numerically,^{20,21} and experimentally.^{22–24} Ruotolo *et al.*,²³ for example, observed the synchronization of four closely spaced vortex-based STNOs with no need of external field, whereas Houshang *et al.*²⁴ recently demonstrated the synchronization of five STNOs by controlling through a combination of Oersted field and external in-plane field, a highly directional spin-wave beam.²⁵ Concerning synchronization of SHOs, Demidov *et al.*²⁶ demonstrated the injection locking^{27–29} of an SHO to a microwave current, while the synchronization of two nanoconstriction-based³⁰ SHOs has been predicted by Kendziorczyk and Kuhn.³¹

In this paper, we predict a strategy that permits to achieve a scalable (in terms of number) synchronization of SHOs, considering a generalization of the geometry introduced in Ref. 11. Our key result is that synchronization always takes place when the distance between SHOs is not large enough. In other words, the magnetization precession of all the involved spins is frequency locked for the whole range of current starting from the critical excitation value. This behavior is linked to the mechanism driving the synchronization that is the magnetodipolar coupling. Synchronization is also robust against geometrical variations of the oscillators and/or the effect of the interfacial Dzyaloshinskii-Moriya interaction (IDMI).³² The synchronized mode is characterized by a unique radiation pattern, as large as the number of synchronized oscillators increases. This result is very promising for the realization of spin wave generators in magnonics applications. Although the synchronization of five SHOs is presented in detail here, the number can be increased to a much larger value.

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Figs. 1(a)-1(c) display the geometrical details of the two devices under investigation, and two and five SHOs are built on top of a Pt(3)/CoFeB(1)/Ta(4) (thicknesses in nm) multilayer with a rectangular cross section of $1500 \times 3000 \text{ nm}^2$. Different from the typical heavy-metal/ferromagnet/oxide layered structure of an SHO, here, the ferromagnet (CoFeB) is sandwiched between two heavy metals (Pt and Ta). This option arises from the need to reduce the critical current to excite propagating modes in an SHO that are still not observed experimentally. In fact, in this system, the spin-Hall effect (SHE) efficiency is increased. Pt and Ta have an opposite sign of the spin-Hall angle and, as demonstrated by Woo et al.,³³ the top and bottom interfaces work in concert and enhance the total torque on the magnetization (typical values of spin-Hall angles for Pt and Ta are $\sim +0.08^{34}$ and ~ -0.15 , size respectively, whereas a total spin-Hall angle of 0.34 was observed in the sandwiched configuration).³³ To realize an SHO in this system, two triangular Au contacts (150 nm thick) are deposited on top (similarly to the strategy developed in Ref. 11); in this way, the current is locally injected in the center of the ferromagnet.¹² The realization of N oscillators can be made through N couples of contacts (see Fig. 1(b)). The distance between each couple of contacts, namely between each oscillator, is indicated with d_c and, in this paper, we show the results for $d_c = 400$ and 800 nm. Distances between contacts are indicated with d_i (i = 1, ..., 5) and are differentiated in order to model fabrication induced geometrical differences in an array of SHOs. As reference, in the paper by Demidov et al.,¹¹ the distance between the contacts is 100 nm; in our study, we choose $100 \text{ nm} \le d_i \le 200 \text{ nm}$. In detail, for the device with two contacts, we analyze four different cases: (*i*) $d_1 = 100 \text{ nm}, d_2 = 200 \text{ nm}, d_c = 400 \text{ nm};$ (*ii*) $d_1 = 100 \text{ nm},$ $d_2 = 110 \text{ nm}, d_c = 400 \text{ nm};$ (*iii*) $d_1 = 100 \text{ nm}, d_2 = 150 \text{ nm},$ $d_{\rm c} = 400 \,{\rm nm};$ and $(iv) \quad d_1 = 100 \,{\rm nm}, \quad d_2 = 200 \,{\rm nm},$ $d_{\rm c} = 800$ nm. On the other hand, the device with five oscillators is characterized by $d_1 = 170 \text{ nm}, d_2 = 200 \text{ nm},$ $d_3 = 100 \text{ nm}, d_4 = 150 \text{ nm}, d_5 = 120 \text{ nm}, \text{ and } d_c = 400 \text{ nm}.$ In previous studies we already identified that in this kind of SHOs propagating spin waves are excited with an out-ofplane external field (see inset of Fig. 1(c)) larger than $200 \text{ mT.}^{12,37}$

Micromagnetic simulations are performed by means of our self-implemented code³⁸ that solves the Landau-Lifshitz-Gilbert equation of motion, where the SHE is included as an additional term modeled as Slonczewski-type torque^{5,37,39}

$$\frac{d\mathbf{m}}{d\tau} = -\mathbf{m} \times \mathbf{h}_{\text{EFF}} + \alpha_G \mathbf{m} \times \frac{d\mathbf{m}}{d\tau} - \frac{g\mu_B}{2\gamma_0 e M_{\varsigma}^2 t_{CoFeB}} \alpha_H \mathbf{m} \times \mathbf{m} \times (\hat{z} \times \mathbf{J}), \quad (1)$$

where **m** and \mathbf{h}_{EFF} are the normalized magnetization and effective field of the ferromagnet, respectively. \mathbf{h}_{EFF} includes the standard magnetic field contributions, as well as the IDMI and the Oersted field (see its spatial distribution in Figs. 1(d) and 1(e)). τ is the dimensionless time $\tau = \gamma_0 M_S t$, where γ_0 is the gyromagnetic ratio and M_S is the saturation magnetization of the ferromagnet. α_G is the Gilbert damping, g is the Landè factor, μ_B is the Bohr Magneton, e is the electron charge, t_{CoFeB} is the thickness of the ferromagnetic layer, α_H is the spin-Hall angle obtained from the ratio between the spin current and the electrical current, \hat{z} is the unit vector of the out-of-plane direction and J is the spatial distribution of the current density in the heavy metals, computed by averaging the current densities flowing in the Pt and Ta over the two sections, respectively. The IDMI is included in the effective field as h_{IDMI} $=-\frac{2D}{\mu_0 M_x^2}[(\nabla \cdot \mathbf{m})\hat{z}-\nabla m_z],$ where m_z is the z-component of the normalized magnetization and D is the IDMI parameter. The boundary condition for the exchange interaction that takes into account the presence of the IDMI is $d\mathbf{m}/dn = -(1/\chi)(\hat{z} \times \mathbf{n}) \times \mathbf{m}$, where **n** is the unit vector normal to the edge, $\chi = \frac{2A}{D}$ is a characteristic length related to the IDMI and A is the exchange constant.^{36,40} For the simulations discussed in this paper, we have considered the following physical parameters: $M_s = 1 \times 10^6 \text{ A/m}, A = 2.0$ $\times 10^{-11}$ J/m,⁴¹ and interfacial perpendicular anisotropy induced at the boundaries between CoFeB and the heavy metals characterized by the anisotropy constant $K_u = 5.5 \times 10^5 \text{ J/m}^{3,42} \alpha_G = 0.03$, and $\alpha_H = 0.34$.³³ For the simulations



FIG. 1. Sketch of the devices under investigation: (a) two SHOs and (b) five SHOs realized by means of couples of Au triangular contacts over a trilayered stack Pt/CoFeB/Ta (c). Reference systems are also shown. (d) and (e) Oersted field distribution corresponding to (d) 2 SHOs, I = 2.56 mA and (e) 5 SHOs, I = 4.72 mA.

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including IDMI, we have chosen a value of 1.5 mJ/m^2 for the parameter D.³⁷ An external field of 400 mT, tilted 15° with respect to the *z*-axis, is applied to the device and tilts the equilibrium magnetization at about 23° with respect to the *z*-axis. Snapshots of the Oersted field in the ferromagnet are shown in Figs. 1(d) and 1(e) for the devices with two and five SHOs, respectively. These computations are based on the numerical framework already described in the previous works,^{12,37} and they have been performed within a parallel processing framework that has been designed and implemented for accelerating algorithms computation.^{43,44}

Figure 2 summarizes the simulation results of the two SHOs. The output frequencies of the device *vs.* applied current are reported for the abovementioned four cases (i)-(iv), with and without including the IDMI (Figs. 2(a)-2(d)). In any of the four cases and for the whole range of applied currents (starting from the threshold of the self-oscillations), we observe that the spins oscillate at the same frequency (frequency locked), with a spatially dependent phase shift, giving rise to a single frequency peak in the power spectrum (see supplementary material Note 1 for the spatially dependent phase shift). Synchronization still takes place for any

applied current also in the presence of a small variation of out-of-plane amplitude and in-plane field angle (not shown).

Fig. 2(e) shows the results for the case (iii) and highlights that the wave vectors are almost the same along the four directions, where specifically the spin-wave radiation is isotropic (the excitation area is elongated due to the geometry of the contacts). This result, together with the synchronization at any current value, makes the double oscillator comparable to a single oscillator with a wider excitation area (its tunability is about 2-2.5 GHz). Figs. 2(a)-2(d) also show that the frequency of synchronized mode exhibits blue shift as a function of the applied current, as expected for the Slonczewski-like spin-waves. With this regard, Figs. 2(f) and 2(g) show the snapshots of the magnetization configuration for the geometry of case (iii) (corresponding to Fig. 2(c)), without and with IDMI (multimedia view movie 2(f)and 2(g)). In both cases, the radiation pattern is unique. The inclusion of IDMI in the model introduces further nonlinearities in the behavior of the device, and the output frequency shows a non-monotonic behavior (see, in particular, Fig. 2(d)). Concerning the mode profile, it is clearly observed that is nonreciprocal, in agreement with the previous results



FIG. 2. (a)–(d) Magnetization oscillation frequency of two synchronized SHOs for four different configurations of the Au contacts. In each graph, frequencies with D=0 mJ/m² and with D=1.5 mJ/m² are reported. (e) Wave vectors along the in-plane axes for the case in (c). (f) and (g) Snapshots of the magnetization corresponding to the points "f" and "g" indicated in (c) for I=2.56 mA (see movie 2(f) and 2(g)). (Multimedia view) [URL: http:// dx.doi.org/10.1063/1.4967842.1][URL: http://dx.doi.org/10.1063/1.4967842.2]

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on the nonreciprocal spin-wave propagation in the presence of IDMI. $^{\rm 45,46}$

In order to investigate on the phenomenon driving the synchronization, we have also simulated an ideal experiment where the magnetic region between the two SHOs has been cut in order to avoid spin-wave coupling. In those computations, synchronization takes place highlighting the key-role of magnetodipolar coupling as driving phenomenon (see supplementary material Note 2 for the simulations with the cut ferromagnet). This is in agreement with a previous work, where it is shown that synchronization driven by magnetodipolar coupling is characterized by a unique wavefront, as in our cases (see Fig. 5 of Ref. 21). The leading role of magnetodipolar coupling also explains the occurrence of synchronization for all the current values that is linked to the distance d_c between the SHOs. Simulations performed with $d_c = 1600 \,\mathrm{nm}$, scenario where the synchronization is driven mainly by spin wave interactions, in fact, show locking for a limited range of current (see supplementary material Note 3 for an example of unsynchronized state at $d_c = 1600 \text{ nm}$). Synchronization, finally, is also mutual since the frequency of the locked mode is in-between the frequencies of the two single SHOs (see supplementary material Note 4 for the evaluation of the frequencies of the single SHOs).

Since the first work on the synchronization of two STNOs,¹⁶ it was necessary more than 10 years to observe the synchronization of five STNOs. It has required larger contacts, a well-defined spatial alignment, and the intuition of the role of the Oersted field.²⁴ Encouraged by the results of the device with two SHOs, we have performed micromagnetic simulations increasing the number N of SHOs up to N = 5. Our computations show synchronization characterized by similar properties of the 2 SHOs. In particular, Fig. 3(a) shows the frequency of the synchronized mode for N = 5, with and without IDMI. Also, in this configuration, we observe the frequency blue shifts with the applied current and oscillators are synchronized for the whole range of currents (mind that $d_c = 400$ nm). Once again, IDMI distorts the profile of the spin-wave, which, even if it remains unique and continuous, becomes non-reciprocal (see snapshots in Figs. 3(b) and 3(c), and the corresponding multimedia view movie 3(b) and 3(c), for the dynamics without and with IDMI, respectively). On the whole, the excitation area is larger than the case of two oscillators, due to the geometry of the contacts. Different from Ref. 24, in the framework studied in this paper, the Oersted field is symmetric and has a negligible role. This feature promises a propagation of the spin-wave at longer distances that can be useful if spin-wave has to reach other devices on the same ferromagnet, namely, for magnonics applications.

In conclusion, our numerical simulations have demonstrated the synchronization of two and five SHOs. In our geometry, synchronization occurs for the whole range of current if the distance between SHOs is not too large, and, in our case, this critical distance is between 800 and 1600 nm. The main mechanism at the basis of the synchronization is a strong coupling due to the large and long range magnetodipolar fields that in our scenario are largest as compared to the previous works on synchronization. This gives rise to a robust synchronization against differences in the geometry



FIG. 3. (a) Frequency of the magnetization oscillation of five synchronized SHOs without and with IDMI. Distances between contacts are $d_1 = 170$ nm, $d_2 = 200$ nm, $d_3 = 100$ nm, $d_4 = 150$ nm, $d_5 = 120$ nm, and $d_c = 400$ nm. (b) and (c) Magnetization configurations obtained without and with IDMI, respectively, corresponding to the points "b" and "c" indicated in (a) for I = 4.72 mA (see movie 3(b) and 3(c)). (Multimedia view) [URL: http://dx.doi.org/10.1063/1.4967842.3][URL: http://dx.doi.org/10.1063/1.4967842.4]

of the contacts. In the synchronized state, an enlargement of the isotropic/anisotropic radiation pattern in the absence/ presence of IDMI, as a function of the increase in the number of locked oscillators, can be useful for the realization of spin-wave source for magnonics applications. The robust occurrence of the synchronization makes our design of SHOs array scalable for a larger number of oscillators.

See supplementary material for Notes 1–4 with details on the spatially dependent phase shift, the simulations with the cut ferromagnet, an example of unsynchronized state at $d_c = 1600$ nm, and the evaluation of the frequencies of the single SHOs.

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